

11.6 Practice - Classify Conics

Period _____

Classify each conic section and write its equation in standard form.

1) $y^2 + x - 4y - 2 = 0$

$$\begin{aligned} y - 4y &= -x + 2 \\ \cancel{y} + \cancel{-4y} &= \cancel{-x} + \cancel{2} \\ (y - 2)^2 &= -x + 6 \\ (y - 2)^2 &= -(x - 6) \end{aligned}$$

Parabola

3) $5x^2 + 6y^2 + 10x - 24y - 121 = 0$

$$\begin{aligned} 5x^2 + 10x + 6y^2 - 24y &= 121 \\ 5(x^2 + 2x + 1) + 6(y^2 - 4y + 4) &= 121 \\ \frac{5(x+1)^2}{150} + \frac{6(y-2)^2}{150} &= \frac{150}{150} \\ \frac{(x+1)^2}{30} + \frac{(y-2)^2}{25} &= 1 \end{aligned}$$

Ellipse

5) $-x^2 + 10x + y - 20 = 0$

$$\begin{aligned} -(x^2 - 10x + 25) &= -y + 20 \\ -(x-5)^2 &= -y - 5 \\ (x-5)^2 &= y + 5 \end{aligned}$$

Parabola

7) $x^2 + y^2 + 4x - 2y - 8 = 0$

$$\begin{aligned} x^2 + 4x + 4 + y^2 - 2y + 1 &= 8 + 4 + 1 \\ (x+2)^2 + (y-1)^2 &= 13 \end{aligned}$$

Circle

9) $4x^2 + 25y^2 - 16x + 200y + 316 = 0$

$$\begin{aligned} 4x^2 - 16x + 25y^2 + 200y &= -316 \\ 4(x^2 - 4x + 4) + 25(y^2 + 8y + 16) &= -316 \\ \frac{4(x-2)^2}{100} + \frac{25(y+4)^2}{100} &= \frac{100}{100} \\ \frac{(x-2)^2}{25} + \frac{(y+4)^2}{4} &= 1 \end{aligned}$$

Ellipse

$$\begin{aligned} x^2 + 4x + 4 + y^2 - 8y + 16 &= -13 + 4 + 16 \\ (x+2)^2 + (y-4)^2 &= 7 \end{aligned}$$

Circle

2) $x^2 - y^2 - 2x - 6y - 12 = 0$

$$\begin{aligned} x^2 - 2x - y^2 - 6y &= 12 \\ x^2 - 2x + 1 - (y^2 + 6y + 9) &= 12 \\ \frac{(x-1)^2}{4} - \frac{(y+3)^2}{4} &= 4 - 9 \\ \frac{(x-1)^2}{4} - \frac{(y+3)^2}{4} &= -1 \end{aligned}$$

Hyperbola

6) $-x^2 - 12x + y - 34 = 0$

$$\begin{aligned} -(x^2 + 12x + 36) &= -y + 34 \\ -(x+6)^2 &= -y - 2 \end{aligned}$$

$$\begin{aligned} (x+6)^2 &= y + 2 \\ (x+6)^2 &= y + 2 \end{aligned}$$

Parabola

8) $x^2 + y^2 - 8x - 4y + 11 = 0$

$$\begin{aligned} x^2 - 8x + 16 + y^2 - 4y + 4 &= -11 + 16 + 4 \\ (x-4)^2 + (y-2)^2 &= 9 \end{aligned}$$

Circle

10) $-9x^2 + 16y^2 - 64y - 80 = 0$

$$\begin{aligned} -9x^2 + 16y^2 - 64y &= 80 \\ -9x^2 + 16(y^2 - 4y + 4) &= 80 \\ \frac{-9x^2}{144} + \frac{16(y-2)^2}{144} &= \frac{80+64}{144} \\ \frac{(y-2)^2}{9} - \frac{x^2}{16} &= 1 \end{aligned}$$

Negative can't be in front. Put this fraction second and make this subtraction between the fractions.

$$\begin{aligned} \frac{(y-2)^2}{9} - \frac{x^2}{16} &= 1 \\ \text{Hyperbola} & \end{aligned}$$